where d_1 is the beam diameter corresponds to the point where the irradiance (I_0) diminishes by a factor of $1/e^2$, and d is the radial distance of a point from the center, similarly, the thermal heat flux is modeled using equation (6) as follows:

$$q(r) = \frac{2P}{\pi r_0^2} e^{-\frac{2r^2}{r_0^2}} \quad (6)$$

where P is the laser power, r_0 the spot radius and r the radial distance.
And the average heat flux on the laser spot is,

$$q_m = \frac{1}{\pi r_0^2} \int_0^{r_0} q(2\pi r)dr = \frac{0.865\alpha P}{\pi r_0^2} \quad (7)$$

where α is the absorption rate.

The laser beam distribution has been assumed to be either surface or volumetric in nature. To avoid the complexity, in [38] the powder has been considered to be a homogenously absorbing and scattering continuum with effective radiation transfer properties equivalent to those of a powder bed. A surface laser beam is common in literature since there is not so much research on laser beam penetration [4,28,39, 38]. In [4], a ray tracing (RC) model has been formulated in which the geometry and structure of the powder have been taken into account. Figure 2 is the two-dimensional (2D) illustration of the model. As shown in figure 2, the laser beam is taken as the ray which penetrates into the powder bed, which is reflected and absorbed by the powders. This experiment was based on the simulation of a large number of rays. This model allows for calculation of the ratio of the total absorption with respect to the material absorption, laser beam penetration, and more. In [39], a volumetric line heat source has been considered with the energy characteristics shown as (8)

$$E_L = \frac{P_L}{v_s}, E_F = \frac{P_L}{h_s v_s} \quad (8)$$

where E_L is the line energy, E_F is the area energy, P_L is the laser power, v_s is the scan speed, and h_s is hatch spacing. In [28], a radiation transfer equation has been used with an isotropic scattering term to describe penetration in metallic powder. And in [7], it was concluded that if the finite element size is larger than five gradient diameters, laser penetration can be ignored in general.

Understanding of the interaction between the powder bed and laser beam is key to the laser penetration and powder bed absorption. Since the absorption parameter are not known accurately, in [16] a constant absorption ratio of pure titanium powder at the Nd-YAG laser wavelength (1.06 mm) was assumed. This assumption has been reported in [48] which also utilizes the absorption ratio for the bulk material. Similarly in [40, 41, 42] a constant absorption rate has been assumed in their modeling schemes. The laser energy absorptance of a material is known to depend on a number of factors such as the nature of the surface, level of oxidation, the wavelength of the incident laser beam, surface temperature, etc [43]. Though, in the case of metallic powders, the absorption ratio varies from the in-coupling absorption as proposed by Kruth et al [5] to within a few percent of the molten metal absorption ratio [20].

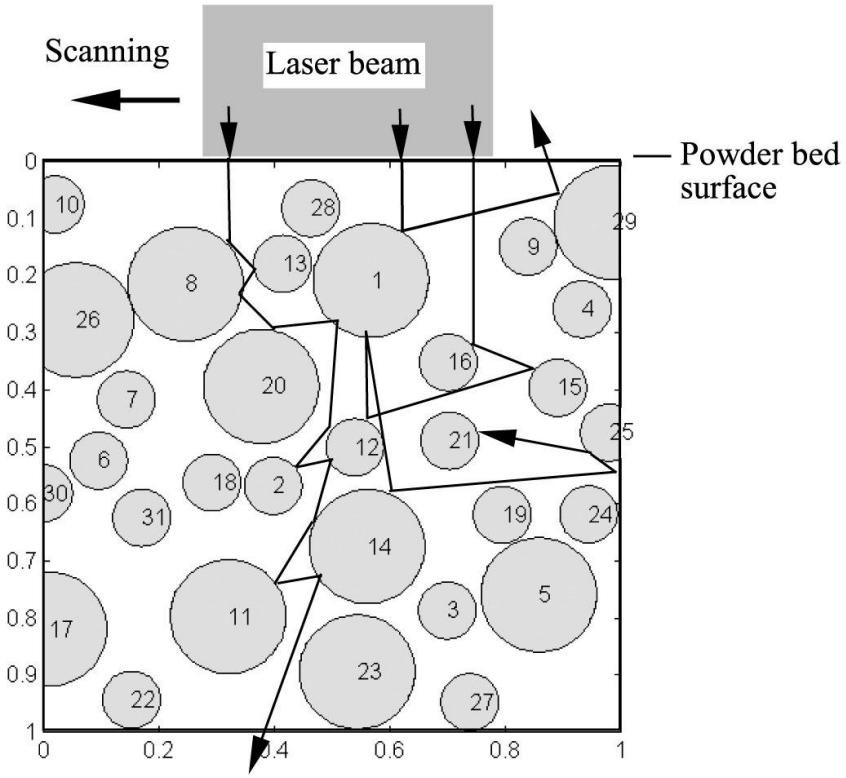

Figure 2 2D illustration of the RC model: simulation over a depth of 1mm and width of 1mm of powder bed [29]

Thermal properties include density, thermal conductivity, heat capacity and enthalpy. In [19], it was shown that thermal conductivity is not a constant value and seems to vary with temperature. In SLM, the effective thermal conductivity has been used. Many formulations were developed using reasonable assumptions or experimentation and it has been established that the powder bed porosity influences conductivity. The effective thermal conductivity is a function of solid and gas thermal conductivity [1,16, 75]. In [1], using the Yagui and Kunni (1989) function, the thermal conductivity of the material $k_e$has been expressed as (9)

$$k_e = \frac{\mu k_s}{1+\Phi\frac{k_s}{k_g}} \qquad (9)$$

where k_s is the conductivity of the solid material, $k_g$is the conductivity of air, μ is the solid fraction($\mu = \frac{\rho}{\rho_s}$)and Φ is an empirical coefficient.

In [44], it has been proposed that thermal conductivity depends on porosity and pore geometries and it is controlled by the amount of gas content inside the pore. In [45], during their studies on light extinction in powder beds, it has been demonstrated that the effective thermal conductivity of a powder is essentially independent of material but depends on the size and morphology of the particles and the void fraction, as well as on the thermal conductivity of the gaseous environment. In [16], it has been established that the thermal conductivity of Ti6Al4V starts off from a low conductivity value for powder material and rises sharply at it nears the melting point. The thermal conductivity of this alloy increases considerably with temperature above room temperature. The temperature range near the melting point and above is the most important for the problem under consideration. In absence of any reliable experimental data, a constant value of k_d = 20 W/(m K) has been assumed, which is obtained by extrapolation to the melting point. The effective thermal conductivity of loose metallic powders is controlled by

gaseous content in the pores [28]. The density and heat capacity of alloy powder can be described as the mean of the individual components in [75].

Analytical solutions

The Carslaw and Jaeger [19] heat transfer model discussed above includes the unusual boundary conditions, and there is no analytical solution which completely satisfies the linear governing equation. However, there are some solutions associated with the simplified model which were first used in welding [46]. In particular, the Rosenthal solutions for a point and line heat source have been proved to be extremely useful in laser-based manufacturing.

The three dimensional (3D) Rosenthal's point solution for temperature distribution using a steady state point heat source moving on the surface of a semi-infinite plate along the x axis is given by (10)[2]

$$\bar{T} = \frac{e^{-(\bar{x}_0 + \sqrt{\bar{x}_0^2 + \bar{y}_0^2 + \bar{z}_0^2})}}{2\sqrt{\bar{x}_0^2 + \bar{y}_0^2 + \bar{z}_0^2}} \qquad (10)$$

where

$$\bar{T} = \frac{T - T_0}{\left(\frac{\alpha Q}{\pi k}\right)\left(\frac{\rho c V}{2k}\right)}$$

$$\bar{x}_0 = \frac{x_0}{2k/\rho c V}\,, \bar{y}_0 = \frac{y_0}{2k/\rho c V}\,, \qquad \bar{z}_0 = \frac{z_0}{2k/\rho c V}$$

The 2D Rosenthal's line solution for the temperature distribution using a steady state line heat source moving on the surface of a semi-infinite plate along the x axis is given by (11)[47]

$$T = T_0 + \frac{Q}{k} line(x', y') \qquad (11)$$

where

$$line(x', y') = \frac{1}{2\pi} \exp(x')\, K_0\left(\sqrt{x'^2 + y'^2}\right)$$

$$x' = \frac{Vx}{2k}, y' = \frac{Vy}{2k}$$

and $\alpha, Q, V, \rho, c, k, K_0$ are the absorption rate, laser power, scan velocity, density, heat capacity, thermal conductivity and the modified Bessel function of the second kind and order zero.

The Rosenthal's solution plays an important role in the study of SLM temperature distribution. A more complicated solution for different laser beam distributions can be built upon these elementary solutions. In [46], the temperature distribution of a moving Gaussian distribution heat source has been derived. The influence of beam diameters has been included, though the solution was in the form of an integral and not a closed form solution. These scenarios can be extended to cover time dependent situations. The one-dimensional (1D) form of a time dependent point and line solution is derived in [47]. In [48], an expression of temperature distribution for a Gaussian heat source in a laser deposition process by using a Green function has been provided. Also, an analytical closed form solution for the maximum temperature of a stationary laser beam, an extremely fast moving laser beam and a laser beam with intermediate velocity has been derived. In [49], a semi-analytical model has been

developed to estimate the thermal field created at a sample surface during a pulsed Nd-YAG laser treatment with constant thermal properties and a laser beam with Gaussian distribution. In [18], equation (1) has been solved analytically with boundary conditions provided in equation (4), the solution strategy ignores other important boundary conditions, such as convection, radiation, etc. From the literature, there are no analytical solutions for the complete problem without considering the nonlinearity of the thermal properties. There are some of the closed form analytical solutions such as the Rosenthal solution for very simple problems. The closed form solution transforms into an integral for more complex boundary conditions. Although these analytical or semi-analytical solutions are very important in the thermal study of SLM, they have many limitations. These solutions, though simple, can help lead to a better understanding of the problem before resorting to more complicated computational methods [47]

Numerical Solutions

Numerical methods are generally used for solving complex problems when closed-form solutions are not available for a physical situation. A number of research groups have reported their simulation strategies and results in the literature and are enumerated in Table 1. . The simulation strategies can be classified by model dimensions, linear/nonlinear approaches, substrate characteristics and laser beam characteristics. The computation time for a real comprehensive model which considers all the factors above is very large and it takes hundreds of hours to compute a 3D model with several layers of real-time SLM processing.

Table 1: Summary of simulation model from literature review

Reference	Material	Basement	Model size: mm	Element size: mm	Laser popup: w	Scan speed: mm/s	Hatch space: mm	Laser beam: mm	Laser type
50	Nickel alloy	N	1.6x(5,10,20)x3.75	0.25	1000	4	0.75	0.75	N/A
51	titanium	N	0.1x0.1	12.5e-3	2	1	N/A	50e-3	Gaussian
7	titanium	N	Coarse: 5x5x2	Coarse:0.1	2	1	0.1	25	N/A
			Fine: 2x2x0.5	Fine:0.01					
40	Cu	N	Height:10	N/A	50-2500	N/A	N/A	0.8	Uniform
52	iron	N	0.03x0.9x0.9	7.5e-3	2,3,4	180,200,225	0.0225	0.03-0.06	Gaussian
8	W-Ni-Fe	Metal: 2x3x1.5	1x2x0.05	0.05	100	20-140	0.05-0.15	0.05	N/A
16	titanium	Mild steel: 3x3x3	1x1x0.15	0.025x0.025x0.03	120	220	N/A	0.1	Gaussian
41	copper	4.8x2x0.5	3.4x1.6x.3	0.1	400	60,120,180	0.3	0.4	Gaussian
53	H13 hot work tool steel	mild steel	20x20x9	N/A	80	500	N/A	0.1	N/A
42	titanium	stainless steel 25x10x5mm	2x1x0.05	5e-3	110	200	N/A	0.034	Gaussian

29	42CrMo4	100x50x5mm	N/A	17675 elements	3500	10-30	N/A	Wide band:10x83x1	Rectangular
30	ceramic	N	20x24x2	0.2	10	3.3	N/A	2	Gaussian

The finite element (FE) and finite difference (FD) methods are the most commonly used numerical methods for solving the SLM thermal problem. A 1D model has its advantages for saving computation time and an ability to reflect some of the main characteristics of the SLM thermal problem. Henceforth, it has been employed commonly in the literature. In [54], a 1D FE model has been developed to simulate the SLS process using Bisphenol-a polycarbonate, and the solution was determined using a basic feed forward FD method. In [40], the axisymmetric heat conduction problem involving the melting of Cu with a pulsed laser source has been solved using a traditional backward difference scheme and Galerkin's FE formulation. The FE mesh has been reconstructed from the change of molten pool shape. In [28], a single line scan on a layer of unconsolidated steel 316L powder has been studied by considering other heat transfer mechanisms such as the radiation and convective heat transfer. The temperature distribution of a single track of laser scanning on the Ti6Al4V powder was studied by including the temperature dependent thermal conductivity and heat capacity in ANSYS [42]. In [29], the thermal field of a wide band laser heat source scanning a single track has been studied and the heat source is considered volumetric.

The 2D model is extensively developed and discussed. A 1D model is not always enough to explore the details of the thermal properties. The 2D model is not as time-consuming and expensive to produce as 3D, and keeps more details than the 1D model. So the 2D model is often appropriate and useful. In [1], the temperature field is described by a quasi steady state equation which has been numerically solved by using the stream upwind Petrov Galerkin (SUPG) strategy together with a shock capturing scheme. In [50], a 2D FE model for a single nickel layer formed on the powder bed by SLM has been derived through the Galerkin method with the backward difference scheme. In [7], the FE method for space discretization coupled with a Chernoff scheme for time discretization, which was proved in [55] that this method provides a fully converged solution to the model, is employed to predict the temperature distribution on the top surface of a titanium powder bed during laser sintering of titanium powder. The quasi regular mesh with fine laser spot area cells and coarse cells in neighbor areas was employed to relieve the computation burden. [56] reports a FE model to simulate the temperature field of polymer-coated molybdenum powder in the SLS process. The model was solved using FORTRAN with fine and coarse meshing. The relative error between the experiment and numerical simulation results were less than 5%. In [51], a 2D non-linear heat transfer with volume internal heat source problem is numerically solved based on the coupling of Matlab and ANSYS FEM models. The phase change effect, effective thermal conductivity, heat capacity and the Gaussian laser energy as internal heat source were considered in this model. The model was spatially discrete by Galerkin FE formulation and time discrete by implicit FE method. [8] predict the surface temperature distribution during SLM of 90W–7Ni–3F materials. [52,53,30] report their research results of temperature fields in single metallic layer SLM processes by using element birth and death.

The 3D model is able to better reflect the real SLM process and provides more information about the thermal field. In [39], a macroscopic FE-model using three different geometries and a volumetric line heat source has been presented. The 3D model shows the sintering of a single line, whereas two dimension models are used for longitudinal and crosscuts

of the sintering process. In [16], a more comprehensive understanding of the SLM thermal field has been achieved by creating a 3D model and considering the interval time (1s) for new powder recoating. A 10% convergence test was conducted to ascertain the suitability of the chosen mesh divisions. In [41], the substrate is included into a 3D thermal model which has three layers of powder. In [57], it takes several hours to simulate a 0.6x0.5x0.5mm cuboid using ABAQUS. It was concluded that using 2D analysis with generalized plane strain conditions seems to be convenient, but 3D analysis remains absolutely necessary to full understand the problem.

Thermal measurements

Analytical and numerical models have limitations when predicting the thermal field in SLM since assumptions are necessary to simplify the problem. These models help researchers understand the process, however, to comprehensively understand the SLM thermal problem, measurements of temperature distribution during SLM are needed to validate the assumption and results. Experimental temperature measurement helps to better understand the interaction between the laser beam and powder bed [5]. Thermal imaging methods have been used numerous times for the determination of temperatures and the results have been published in different papers and theses [7,16,56,58 ,59,60]. However, the system is affected by the distance of the infrared device and powder bed. [7,16,56,59,60] set up the temperature measurement system to compare and validate their simulation model result by using an infrared camera. The top surface average temperature of titanium powder was measured in [59] under the continuous and pulsed wave modes of an Nd:YAG laser. The results show that the average powder bed surface temperature using pulsed wave mode is 30% lower than the continuous wave mode. Also, consolidation in pulsed wave mode is much more efficient than continuous wave mode. However, cameras were not able to resolve the temporarily higher skin temperature rises. The same experiments were carried out [7] for titanium power. Temperatures less than 500 ^{o}C were not presented since the camera data was not reliable below that threshold. The infrared camera resolution used in [7,59] was 256x256. [56,60] build an infrared thermometer to measure the powder surface temperature, and use the thermocouple to test the interior temperature of polymer-coated molybdenum powder in the SLS process. However, [7,56,59,61] do not describe details of their systems like implementation, camera angle, etc. In [58], a temperature monitoring system for a laser sintering system is presented and it explains the importance of the angle between the camera's axis and surface normal. Some reference papers in [58] from Europe analyze the influence of this angle and experiments have been done to measure the temperature using different angles. For this experiment a thermal imaging system was built into a DTM Sinterstation 2500. The thermal system uses the InfraTec Jade III MWIR with an optical resolution of 320x240, which is able to measure the whole powder temperature and also the melting temperature of the molten pool.

[62,63,64,65] develop feedback temperature control systems to ensure a homogenous temperature field and stable molten pool. A CMOS camera based control loop system is used in [62] to measure the melt pool size and control for overhanging structures. The controller bandwidth was only applied to limited scan velocities. [63,64] improve the controller to be able to monitor the melt pool continuously at high speed through the building process in real time. The thermal monitoring system was a combination of two types of optical sensors – a 2D digital CCD camera and a single spot pyrometer based on photodiodes [65]. Both monitoring systems were developed and used for the SLS/SLM process according to their different laser spot sizes.

Process parameter effects and optimization

The quality of laser sintered parts greatly depends on proper selection of the processing parameters, such as laser power, scanning speed, spot size and material. These have significant influence on the temperature distribution in the powder bed. A homogenous temperature field can lead to better microstructure, mechanical properties, dimensional accuracy and surface finish. Researchers typically try to find a relationship between process parameters and the temperature field. Simulation models and design of experiment methods are the two most common ways to evaluate effects and correlations. The simulation results from [8,41,52,66] conclude that the peak temperature will increase with higher laser power and lower scan speed. These phenomena result from the increasing energy density corresponding to higher laser power and lower scan speed. T.C. Child and C. Hauser in [52,66,67] create a single track process map, shown in figure 3. The whole map is divided into five areas and each represents the 314SS single track shape with different laser power and scanning speeds. A preheating and narrower scan interval will increase the peak temperature [8]. In [41], the study shows that the surface quality of a single sintered layer will improve by lower scanning speed; however, higher scan speed is needed to improve the multi layer surface quality.

Experimental design methods are usually used to test the process parameter effects and predict the temperature using a database collected from experiment or simulation. Part density is predicted in [68] as a nonlinear function of several process parameters in SLM by response surface methods. The data is from a simulation model based on ANSYS. Central composition design is used in [69] to predict the density, hardness and porosity of sintered low carbon steel parts under a pulsed Nd:YAG laser. The design shows that increasing layer thickness and hatching distance results in an increase in porosity and decrease in the hardness and density [69]. [70,71] use EFCP2^3 and central point to study how process parameters effect single tracks and single layers in SLM.

Classical design of experiment methods need a large numbers of data. Some advanced intelligence methods can make predictions using smaller databases. The neural network method is one advanced method from the literature [72,30]. In [64], it is used to build a model based on a feed-forward neural network (NN) with a back propagation (BP) learning algorithm. The basic idea is to train the prepared database first and then use the NN algorithm to create a good mapping between the process parameters and their resulting properties. Then the system can help to determine the most suitable process parameters automatically. In [73], an iterative method to optimize non-linear processes was developed. This neural model is able to make adjustment of the four process parameters with regard to target values of three product properties. The method is applied to SLM of titanium powder.

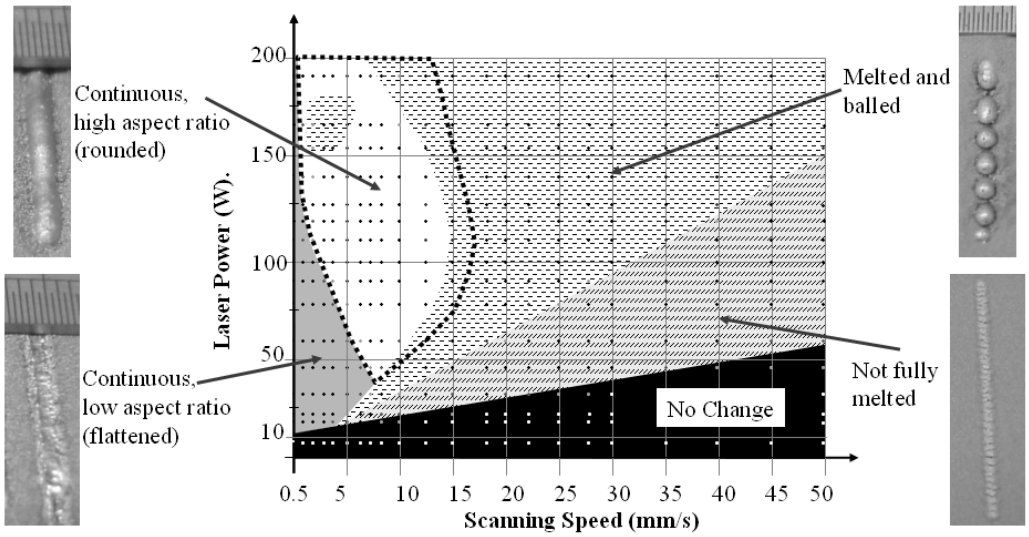

Figure 3 314S single track process map produced using a laser spot size of 1.1mm [52]

Case study

This section uses a model to show some characteristics of the SLM thermal field. The model in this study represents building Ti6Al4V on a Steel substrate, which is shown in Figure 4. The process parameters and Ti6Al4V thermal properties are adopted from [16]. The material is mild steel from [42]. The model and process parameters are shown in table 2. The simulation is carried out in ANSYS. The laser beam is assumed to have a Gaussian distribution with spot size 100 μm. The element size is one quarter of the laser diameter and the laser energy is distributed on a 4X4 grid at every load step. The scanning strategy is the traditional S pattern. Convective heat and radiation in the molten pool is neglected [16]. Laser power and substrate surface heat convection are considered and the initial temperature is set at 335K.

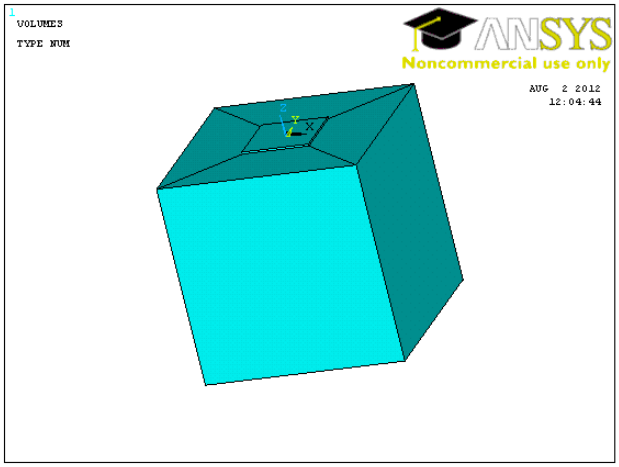

Figure 4. 3D model with substrate

The model simulates one powder bed layer. The temperature profile for the first layer is shown in figure 5, in which the scanning direction is from right to left. The temperature isotherm

curve is a series of ellipses, which agrees with the result in [8]. The contour plot also shows that the front end of the molten pool is denser than the back end, that is, the thermal gradient at the front of the molten pool is larger than the back when considering laser scan direction. The reasons are mainly because of the different material thermal properties since they are temperature dependent and the thermal conductivity is increasing with increasing temperature as well as the fact that the laser source is moving.

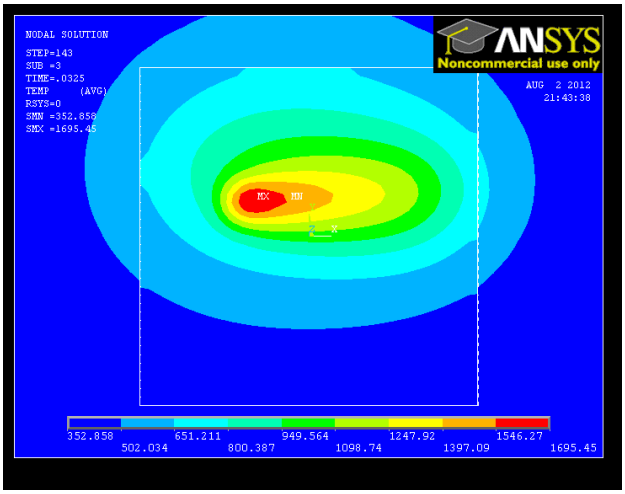

Figure 6 Temperature profile at 0.0325s

Temperature variation with time is shown in figure 7. Figure 7(a) shows that for one track scanning there is only one temperature peak. Figure 7(b) shows temperature variation for single layer scanning. There are three temperature peaks. The laser scanning is following a traditional S pattern as it scans back and forth. As such the laser will heat the same position three times per layer, which leads to rapid temperature increases and drops three times. The number of peaks is determined by the laser spot diameter and hatch spacing. From figure 7 can be observed that the temperature increase rate is higher than the cooling rate. One important phenomenon is that the peak temperature happens after the laser beam has passed the spot. There is a lag between the laser beam and peak temperature. The red line in figure 7 illustrates the time when the laser beam passes, and it can be seen that the peak temperature happens after the beam has passed.

Table 2 Model information and process parameters

Process parameters			
Laser power	120w		
Laser type	Gaussian distribution		
Spot size	100 μm		
Scanning speed	220mm/s		
Powder size	30 μm		
Hatch space	50 μm		
Absorption rate	0.35		
Model information			
	Material	Dimension(mm)	Meshing(mm)
Block	Ti6Al4V	3x3x3	free
Substrate	Mild Steel	1x1x0.03	0.025x0.025x0.03

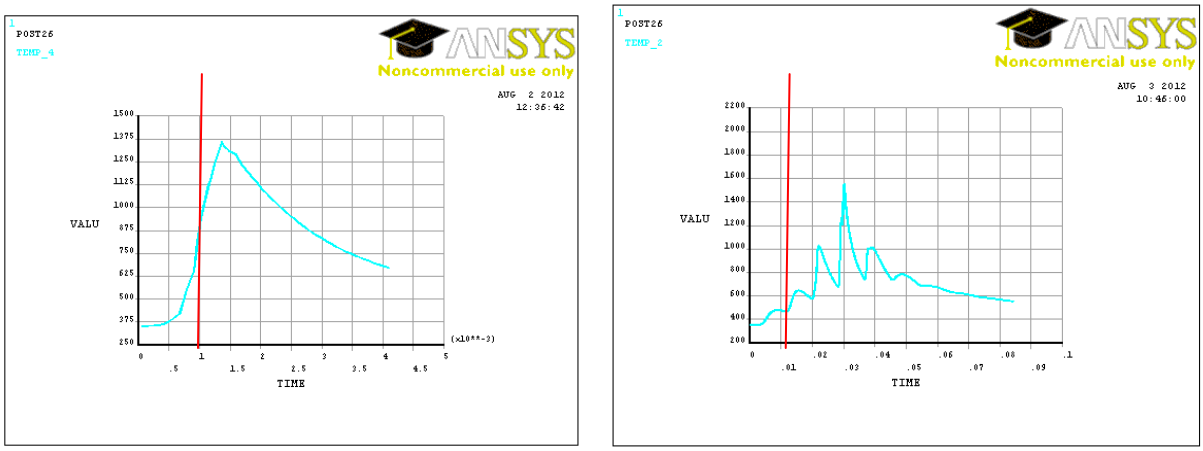

Figure 7 Temperature variation with time for one track scan (a), temperature variation with time for one layer scan (b)

The pictures shown in Figures 8 and 9 are the process parameter effects of laser power and scan speed. The peak temperature increases with higher laser power and lower scan speed which has been shown in [8,41,52,66]. This can be explained by the laser energy; the higher power can generate more energy, as can lower scan speed.

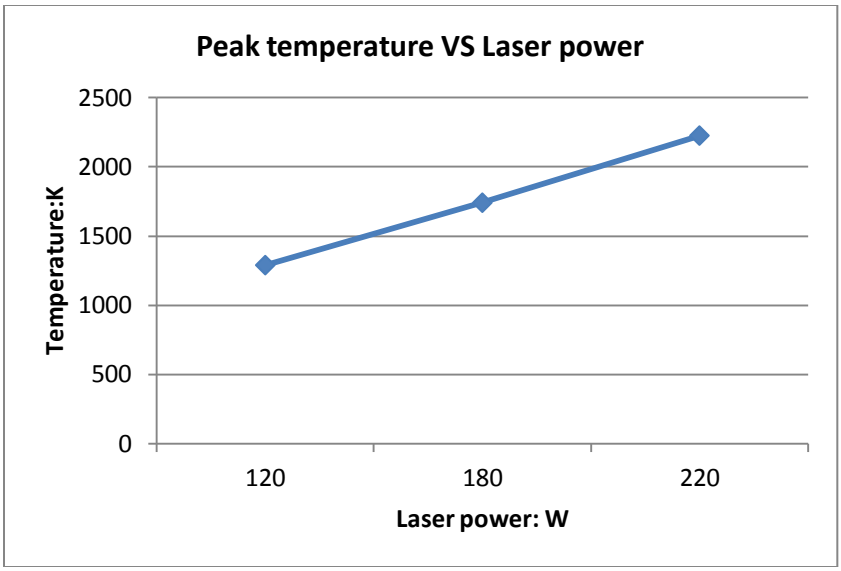

Figure 8 The influence of the laser power to peak temperature

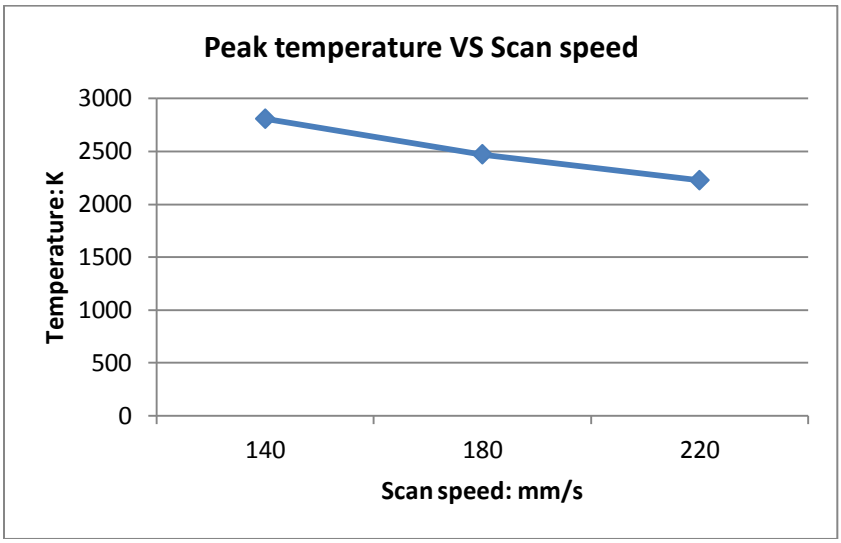

Figure 9 The influence of scan speed to peak temperature

Conclusion and future discussion

A comprehensive literature review of the thermal modeling method in laser sintering is presented in this paper. Classical Fourier heat transfer equations are the most common for describing the temperature distribution. Based on the Fourier equation, various models have been developed by combing latent heat, material thermal property nonlinearity, laser heat source distribution and interaction between a laser beam and powder bed[21,22,23,24,25,26,27]. Many models consider the influence of sintered part shrinkage, molten pool liquid flow and binding mechanism [32,33,34,35,36,37,74]. None of these models can be completely solved analytically. Numerical methods are employed extensively to solve the temperature distribution problem where the FE method has proven to be reliable using available commercial software. Finally, temperature measurement systems have been used to demonstrate the actual temperature distribution in SLM processes to compare against the models.

Great efforts have been put into the field of SLM thermal analysis since the emergence of SLM technology, but there are still many areas of improvement that are needed, including in analytical and simulation modeling as well as in the experimental measurement and control side. A better understanding of SLM sintering and binding mechanisms will lead to better modeling of the SLM thermal field. Better understanding of the input energy model, which includes laser beam distribution, energy penetration and material absorption ratio; and the thermal properties, such as thermal conductivity, density of powder before and after laser scanning, are needed.. From the literature review of various SLM thermal numerical models it can be seen that very few models attempt to represent parts in the same length scales as those which are built in SLM in reality. This is due to the fact that the problem is highly nonlinear, resulting in a heavy computational burden. Future work which carefully chooses an efficient numerical method and which utilizes some form of adaptive meshing technology will be of great help. With improvement in numerical modeling, the optimization of process parameters and exploration of empirical relationship between process parameters and temperature will become easier. These models can then be validated using well-developed temperature measurement systems. In the future, a parametric SLM simulation model which accurately predicts the optimal process parameters or parameter windows will significantly benefit users of laser sintering technology.

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